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## ELECTROOPTICS OF A THIN FERROELECTRIC SMECTIC C\* LIQUID CRYSTAL LAYER

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Abstract The form of ferroelectric smectic C\* electrooptical response vs the layer thickness and the angle  $\beta$  between the polarizer and analyser is investigated. The criterion of the smectic C\* switching rate is proposed and the method for the rotational viscosity measurements is developed.

### INTRODUCTION

The great interest is concentrating in studying the electrooptic effect in thin homogeneously oriented smectic C\* layers, having small thicknesses  $L \sim 1 - 5 \mu$ . In this case the smectic C\* helix pitch  $P_0 > L$  and is unwound due to influence of boundary conditions. This smectic C\* director alignment, defined in<sup>10</sup> as Surface Stabilized Ferroelectric Liquid Crystal Structure (SSFLCS), is characterized by several thermodynamically stable and optically distinguished states with the electrical field switching between them<sup>10 - 12</sup>.

Though the switching rate of ferroelectric liquid crystal (LC) (the speed of electrooptical response) has been investigated in experimen-

tal<sup>3-5,8</sup> and theoretical<sup>9, 12</sup> works, there still does not exist the detailed study of this response in dynamics vs smectic C\* physical parameters and the layer thickness. Consequently, the accurate criteria for measuring the smectic C\* electrooptical response speed are also absent. To fill this gap is the aim of our paper. We also propose the method for determination of the rotational viscosity  $\gamma_{\varphi}$  with respect to rotations  $\varphi$  around smectic C\* layer normal.

### THEORY

Consider a homogeneously oriented layer of a smectic C\* liquid crystal in linear electrooptic effect (Fig. 1). When the electric field  $E$  changes its sign the polarisation  $P_s$  of smectic C\* is also reversed and the director rotates around the layer normal ( $Z$  - axis) to its new state (Fig. 1). While in the initial state the smectic C\* director coincides with the polariser ( $n(-E) \parallel P$ ), in the final state the director  $n(+E)$  forms the angle  $2\theta_0$  with the plane of the polariser. The analyser  $A$ , placed at the angle  $\beta$  with the polariser, provides the variation of the output smectic C\* electrooptic transmission response.

According to phenomenological theory of S.A. Pikin<sup>13</sup>, the director rotation around the smectic C\* layer normal  $Z$  (parallel to the substrates) (Fig.1) may be described as follows:

$$\tilde{\kappa} \theta_0^2 \frac{\partial^2 \varphi}{\partial x^2} + P_s E \cdot \sin \varphi = \gamma_{\varphi} \frac{\partial \varphi}{\partial t} \quad (1)$$

where  $\varphi$  is the rotation angle,  $\theta_0$  - smectic C\* director tilt in the layer,  $\tilde{\kappa}$ ,  $\tilde{\gamma}_\varphi$  - elastic and viscosity constants with respect to azimuthal  $\varphi$  deformations,  $t$  - time.

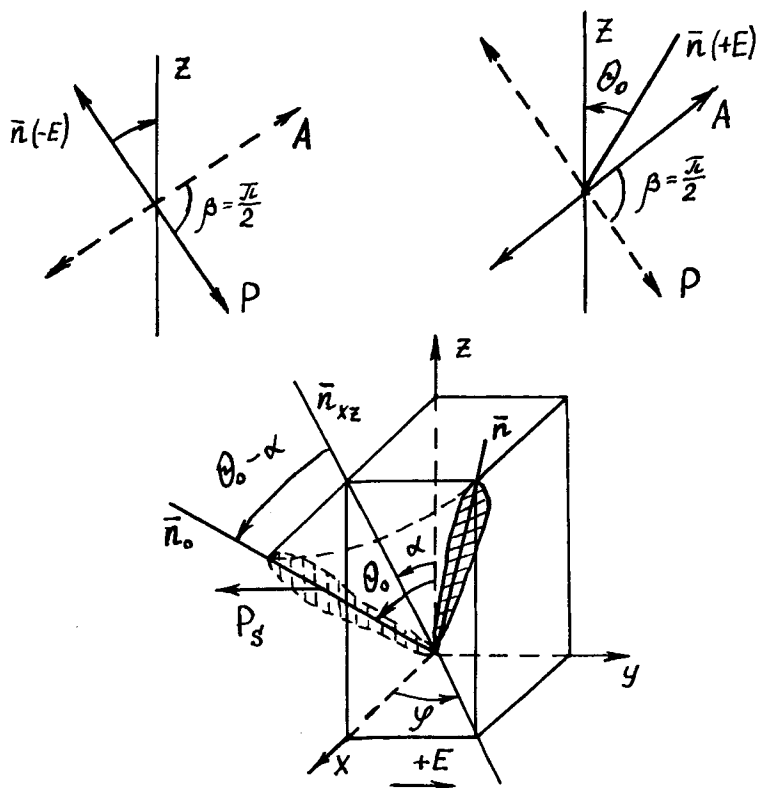


Fig.1. At the top: the location of the polarizer (P), analyser (A) and C\* director angle in the initial  $n(-E)$  and final  $n(+E)$  states.

Bottom: The intermediate position of the director during its rotation around the smectic C\* layer normal.

The equation (1) ignores the variations of the smectic C\* layer tilt angle under the influence

of the electric field  $E$ , which is correct, if the working temperature is not too close to the smectic  $C^*$  - smectic  $A$  transition point<sup>13</sup>. Our qualitative theoretical description also does not take into account the boundary conditions and the elastic term  $\sim \tilde{\kappa} \theta_0^2 \frac{\partial^2 \varphi}{\partial x^2}$  in equation (1). According to<sup>9-12</sup> this is reasonable in case of sufficiently large switching fields. Thus, neglecting the first term in (1) we have:

$$\varphi = \arctg (A \cdot \exp(t/\tau_c)), \quad A = tg \varphi_0/2, \quad (2)$$

$$\varphi_0 = \varphi(t=0), \quad \tau_c = \delta \varphi / \beta E$$

The value of  $\tau_c$  in (2) may be taken as a criterion for the evaluation of smectic  $C^*$  switching rate in linear electrooptical effect.

Since (2) is an approximate solution for the director angle and the constant  $A$  in (2) has no clear physical origin<sup>12</sup>, its value may be chosen from the best matching of theoretical and experimental characteristics of smectic  $C^*$  electrooptic response.

The variation of the optical contrast  $\bar{I}/\bar{I}_0$  ( $\bar{I}_0$  - is the initial intensity level,  $\bar{I}$  - transmitted intensity) in linear electrooptic effect may be described as follows<sup>14</sup>:

$$\bar{I}/\bar{I}_0 = \sin^2\left(\frac{4\theta_0 f^2}{1+f^2}\right) \cdot \sin^2\left(\frac{\Delta\Phi}{2} - \delta_0 \cdot \frac{2f}{1+f^2}\right) \quad (3)$$

where  $f = A \cdot \exp(t/\tau_c)$ ,  $\delta_0 = \frac{\pi L n_a}{\lambda} \left(\frac{n_a^2}{n_s^2} - 1\right) \theta_0^2$ ,

$\Delta \Phi_0 = \frac{2\pi L}{\lambda} \cdot (n_{\parallel} - n_{\perp})$ ,  $\lambda$  - light wavelength,  $n_{\parallel}$ ,  $n_{\perp}$  - smectic C\* refractive indices parallel and perpendicular to the director respectively,  $\beta = \frac{\pi}{2}$  - the angle between the polariser and analyser.

One can use the relation (3) for the approximation of experimental  $I/I_0$  curve, obtained in electrical field switching process (Fig.2).

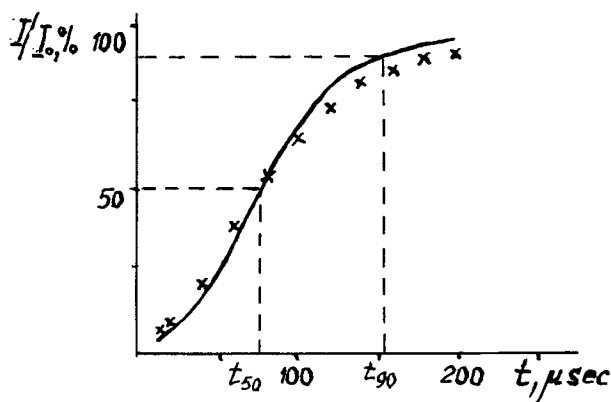


Fig.2. Electrooptical transmission response of DOBAMBC: (x)-experimental data (the external voltage  $U=4\text{v}$ ), solid line - the result of computer fitting procedure by the least squares method with the help of the formula (3). The following parameters are used in the calculations:  $L=5\mu$ ,  $\lambda=0,63\mu$ ,  $n_{\parallel}=1,7$ ,  $n_{\perp}=1,5$ ,  $\theta_0=0,44$ . The computer fitting gives  $A=2$ ,  $\tau_0=95\mu\text{sec}$ , while according to the approximate formula (6) we have  $\tau_c=90\mu\text{sec}$ .

Let us note, that the optical contrast  $I/I_0$  considerably depends on the smectic C\* layer thickness (Fig.3). One can easily show, that for  $L = K\beta / (n_{\parallel} - n_{\perp})$  ( $K=0, 1, 2, \dots$ ) the curve

$I/I_0(t)$  passes through the maximum, while for  $L = (K+1/2) \lambda / (n_H - n_L)$  ( $K=0, 1, 2, \dots$ ) the optical contrast  $I/I_0(t)$  always increases with rising the time  $t$  (Fig.3). Thus the layer thickness non-uniformity  $\Delta L$  within the smectic  $C^*$  electrooptic cell working area must satisfy the requirement<sup>14</sup>

$$\Delta L \lesssim \frac{\lambda}{8(n_H - n_L)} \quad (4)$$

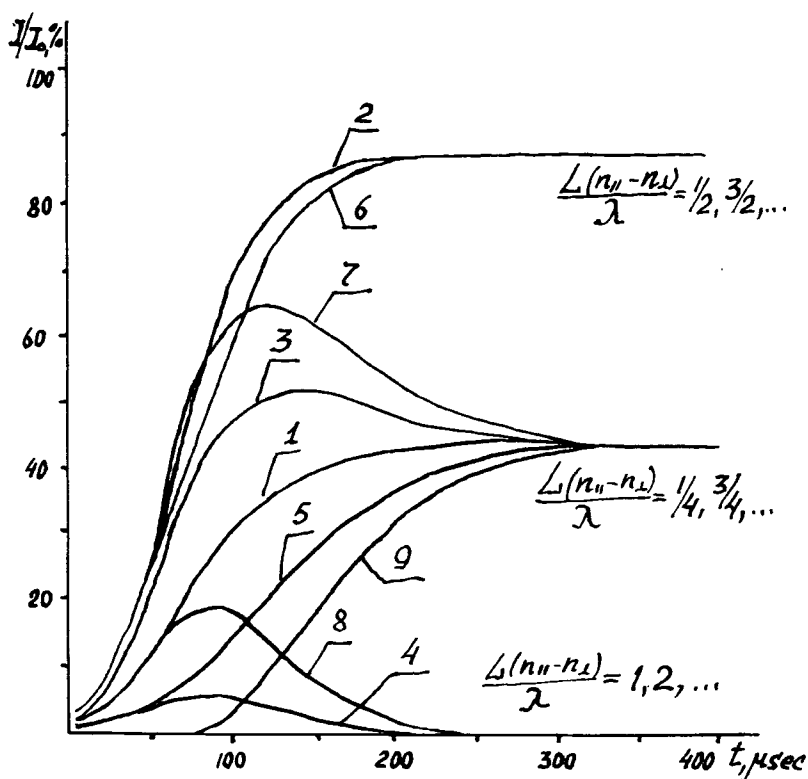


Fig.3. Electrooptical transmission response of ferroelectric smectic  $C^*$  liquid crystal, calculated by means of (3), vs the layer thickness  $L$ . We use in the calculations:  $\lambda = 0,63 \mu$ ,



$n_{\parallel}=1,7$ ,  $n_{\perp}=1,5$ ,  $\theta_0=0,3$ ,  $A=0,43$ ,  $\tau=66 \mu\text{sec}$ ,  
 $L_0 = \lambda / (n_{\parallel} - n_{\perp}) = 3,15 \mu$ . The layer thickness  
 $L = KL_0/4$  ( $\Delta\Phi_0 = \pi K/2$ ), where  $K=1,2$ ,  
 ...9 - the number of the corresponding curve.

The form of smectic  $C^*$  electrooptic response  $I/I_0(t)$  can be affected by varying the angle  $\beta$  between the polariser and analyser (Fig.1). Using the well known formula<sup>15</sup> we have:

$$\left(\frac{I}{I_0}\right)_{\beta} = \cos^2\beta - \sin(4\theta_0 \frac{f^2}{1+f^2}) \cdot \sin(4\theta_0 \frac{f^2}{1+f^2} - 2\beta) \cdot \sin^2\left(\frac{\Delta\Phi_0}{2} - \delta_0 \cdot \frac{2f}{1+f^2}\right) \quad (5)$$

Fig.4 shows, how altering the angle  $\beta$ , one obtains the monotonous rise of the optical contrast for the sufficiently high values of time  $t$ .

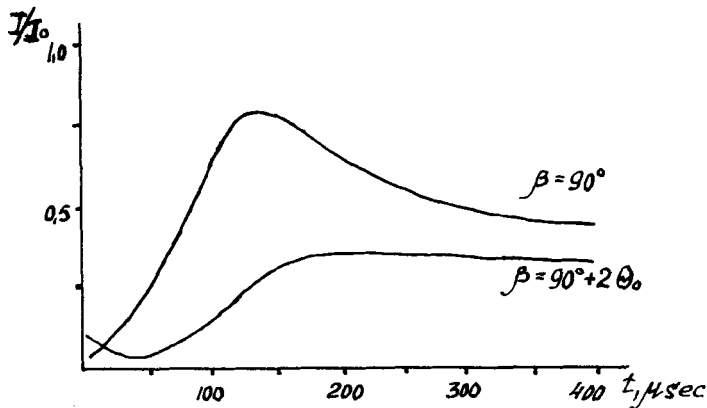


Fig.4. The electrooptical response of ferroelectric smectic  $C^*$  liquid crystal vs the angle  $\beta$  between the polariser and analyser for the curve N7 ( $L=7L_0/4$ ) of Fig.3.

## EXPERIMENTAL AND DISCUSSION

We investigated in experiment the electrooptical transmission response of homogeneously oriented ferroelectric smectic  $C^*$  liquid crystal (DOBAMBC), placed between the polarizer and analyser (Fig.1). He-Ne laser with  $\lambda = 0,63 \mu$  was used as a light source. The external voltage, applied to the cell, was taken in the form of bipolar pulses, which makes it possible to study the dynamics of smectic  $C^*$  transmission after the abrupt change of the voltage sign. The layer thickness  $L \sim 5 - 8 \mu$ .

Fig.2 shows the experimental dynamical transmission curve of DOBAMBC in case, when the phase retardation  $\Delta\phi_0 = \frac{2\pi L (n_1 - n_2)}{\lambda} \sim 3\pi$ . The computer fitting of the  $I/I_0(t)$  electrooptic response with the help of the formula (3) is seen to provide a good agreement with the experimental data. The time constant, obtained by the least squares technique was  $\tau_c = 95 \mu\text{sec}$ .

Using the equation (3) we derive a simple formula for  $\tau_c$ , which makes possible the direct evaluation of  $\tau_c$  without the procedure of computer fitting the experimental  $I/I_0(t)$  data:<sup>14</sup>

$$\tau_c = \frac{t_{90} - t_{50}}{\ln \sqrt{5}} \sim \frac{t_{90} - t_{50}}{0.8} \quad (6)$$

The approximate value of  $\tau_c = 90 \mu\text{sec}$  received by means of (6), matches the value of  $\tau_c$ , taken from the procedure of the computer fitting with the accuracy of 6%.

In experiment we appraised the DOBAMBC di-

director free relaxation time  $\tau_{\text{rel}} \sim 30 - 60$  msec, which is much longer than the characteristic director response time  $\tau_c$  (Fig.2). We also chose the layer thickness  $L$  for which the apparent dynamical threshold was less than 0,5v, while the working voltage was 4v. Then our experimental data may be described within the framework of <sup>the</sup> qualitative theory. According to that, the electro-optical switching rate of smectic  $C^*$   $\tau_c$  was measured by the following procedure. First of all, the appropriate angle  $\beta$  between the polariser and analyser was chosen, to provide a monotonous rise of electrooptic response. Then the characteristic times  $t_{90}$  and  $t_{50}$  were defined, and the value of  $\tau_c$  (6) was calculated.

We also measured the temperature dependence of the smectic  $C^*$  DOBAMBC switching rate vs temperature. Taken into account the well-known temperature dependence of the polarisation of DOBAMBC  $P_s(T)$ , we obtained by means of (2) the corresponding temperature characteristic for the rotational viscosity  $\gamma_\varphi$  (Fig.5).

The rotational viscosity  $\gamma_\varphi$ , measured in our experiment, acts a role of a kinetic coefficient, describing the dynamics of the azimuthal smectic  $C^*$  director angle  $\varphi$  for the fixed polar angle  $\theta_0$ . The paper<sup>16</sup> give the temperature dependence of the another smectic  $C^*$  rotational viscosity  $\gamma_{\theta_0}$ , related to the dynamical relaxation processes of the polar (tilt) angle  $\theta_0$  at a constant value of  $\varphi$  (Fig.6). The comparison of the  $\gamma_\varphi$  and  $\gamma_{\theta_0}$  leads to the conclusion,

that, in general, one deals with the tensor of smectic  $C^*$  viscosity,  $\gamma_\varphi$  and  $\gamma_{\theta_0}$  being its principal components.

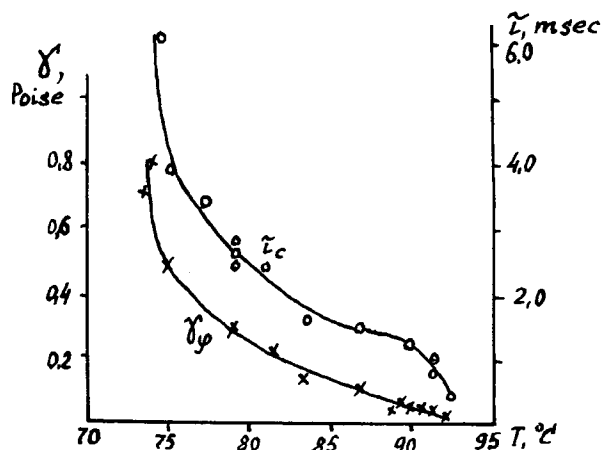


Fig.5. The switching rate  $\tau_c$  and the rotational viscosity of DOBAMBC vs  $^\circ$ temperature. The layer thickness  $L = 7,3 \mu$ . The bipolar rectangular voltage pulses with the amplitude  $U = 2v$  and frequency  $f = 50$  Hz are used in experiment.

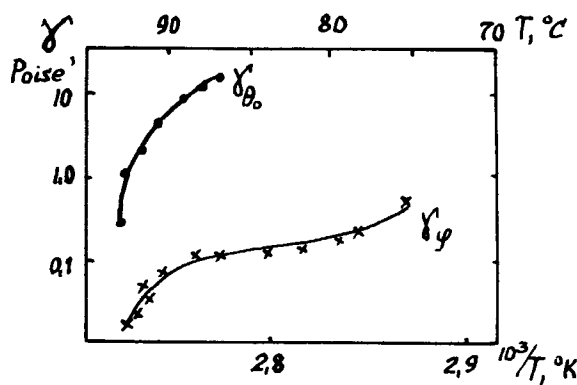


Fig.6. The DOBAMBC rotational viscosities with respect to azimuthal director variations

$\varphi - \delta_\varphi$  and tilt angle  $\theta_0$  ones -  $\delta_{\theta_0}$ .

However, if the  $\theta_0$  variations are small, the electrooptuc response dynamics may be described only with the help of  $\delta_\varphi$  rotational viscosity. Fig.5 and Fig.6 demonstrate, that the  $\delta_\varphi$  compares in value with the typical rotational viscosity of nematic LCs at room temperatures (or even less), while  $\delta_{\theta_0}$  remains by one or two orders of magnitude greater. The small values of chiral smectic  $C^*$  liquid crystal viscosity  $\delta_\varphi$  may be explained by the symmetric peculiarities of smectic  $C^*$ : the dissipation of  $C^*$  free energy process of the director rotation around the layer normal remains reasonably low.

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